

Spring 2001 Released Test

(Supplemental Information)

End of Course

Algebra II

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Introducing the Virginia Standards of Learning

Algebra II

One of the complete test forms from the Spring 2001 Standards of Learning administration is presented in the following pages. The intent of this released test is to provide parents and teachers additional information to accompany the Student Performance Report and/or the Parent Report.

The information accompanying each test question is broken into several components:

Reporting Category: Matches the score report and allows for identification of strengths and weaknesses indicated by student scores.

Standard of Learning: Presents the SOL used in developing the assessment question.

Instruction: Provides information for teachers to use as the SOL is incorporated into instruction.

The answer to each question can be found at the back of the booklet.

2 Which property is illustrated by this

F Commutative Property for Addition

equation?

 $\frac{3}{2}x + 0 = \frac{3}{2}x$

G Distributive PropertyH Additive InverseJ Additive Identity

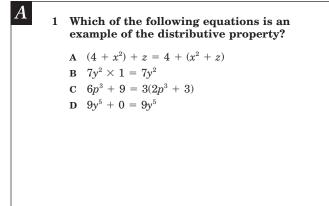
Algebra II



Reporting Category: Expressions and Operations

A. Standard of Learning: A.II.1 The student will identify field properties, axioms of equality and inequality, and properties of order that are valid for the set of real numbers and its subtests, complex numbers, and matrices.

Builds On: Students begin working with properties in the grade 7 SOL and continue through the Algebra I SOL.



Instruction: Provide students an opportunity to identify illustrations of the distributive property, and use the

additive identity property.



A. Standard of Learning: A.II.2 The student will add, subtract, multiply, divide, and simplify rational expressions, including complex fractions.

Builds On: Students begin working with operations with fractions in the grade 3 SOL and continue through the Algebra I SOL.

$A {}_3 \frac{6a+12}{a} .$	$\frac{a^3}{a+2} = ? $ 5	W	Thich is equivalent to $\frac{x^2-4}{x^2-4x+4}$?
A $6a^2$		A	$\frac{1}{x+1}$
B $\frac{6}{a^2}$		в	$\frac{x+2}{x-2}$
$\mathbf{C} \frac{6(a + a)}{a}$	2)	С	$\frac{1}{4x}$
$\mathbf{D} \frac{6a^2 + 1}{\mathbf{D}} = 1$	$\frac{24a+24}{a^4}$	D	$\frac{1}{x+4}$
4 Which is	equivalent to $\frac{3x}{7} + \frac{5y}{14x}$?		
$\mathbf{F} = \frac{8y}{21}$			
$\mathbf{G} \frac{x^2}{14}$			
$\mathbf{H} \frac{6x^2 + 1}{14x}$	<u>5y</u>		
$\mathbf{J} \frac{3x^2 + x}{14x}$	5 <u>y</u>		

Instruction: Provide students an opportunity to simplify rational expressions.

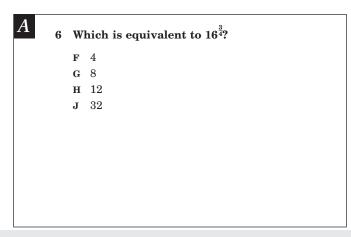




A. Standard of Learning: A.II.3 The student will

a) add, subtract, multiply, divide, and simplify radical expressions containing positive rational numbers and variables and expressions containing rational exponents.

Builds On: Students begin to work with radicals (square roots) in the grade 6 SOL and continue through the Geometry SOL.

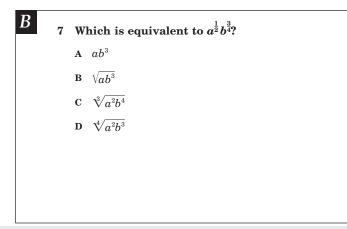


Instruction: Provide students an opportunity to simplify expressions containing rational exponents.

B. Standard of Learning: A.II.3. The student will

b) write radical expressions as expressions containing rational exponents, and vice versa.

Builds On: Students begin to work with radicals (square roots) in the grade 6 SOL and continue through the Geometry SOL.



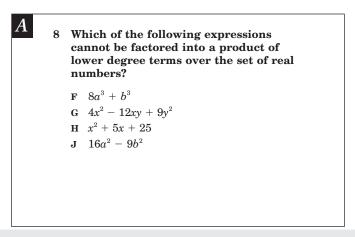
Instruction: Provide students an opportunity to express a product containing rational exponents as a radical expression.





A. Standard of Learning: A.II.5 The student will identify and factor completely polynomials representing the difference of squares, perfect square trinomials, the sum and difference of cubes, and general trinomials.

Builds On: Students begin work with number factors in the grade 3 SOL and with polynomial factors in the Algebra I SOL.



Instruction: Provide students an opportunity to factor a trinomial with two variables and a leading coefficient greater than 1.

B. Standard of Learning: A.II.17 The student will, given a set of data points, write an equation for a line of best fit, using the median fit method, and use the equation to make predictions.

Builds On: Students begin work with performing operations on complex numbers and with polynomial factors in the Algebra II SOL.

B 9 Wha	at is the sum of $(2 - 5i)$ and $(3 + i)$? 10	Which	is equivalent to $\frac{5+i}{1+3i}$?
в 1		$\mathbf{F} = \frac{4}{\xi}$	$\frac{-8i}{5}$
D 5	5 - 4i	$G = \frac{4}{\xi}$	<u>- 7i</u> 5
		н 1-	<u>- 7i</u> 5
		J <u>-1</u>	$\frac{-7i}{4}$

Instruction: Provide students an opportunity to simplify a ratio of complex numbers and add complex numbers.

Algebra II



Reporting Category: Relations and Functions

A. Standard of Learning: A.II.8 The student will recognize multiple representations of functions (linear, quadratic, absolute value, step, and exponential functions) and convert between a graph, a table, and symbolic form. A transformational approach to graphing will be employed through the use of graphing calculators.

Builds On: Students begin to study relations and functions in the grade 7 SOL and progress through to a study of linear and quadratic functions in the Algebra I SOL.

A	11	y y y y y y y y y y y y y y y y y y y	12 $ \frac{x f(x)}{\neg 3 2} \\ 0 5 \\ 3 \neg 10 $ The table shows some elements of a function. Which equation is most likely a rule for the function? F $f(x) = x + 5$ G $f(x) = -5x + 5$ H $f(x) = 5 - 2x - x^2$ J $f(x) = x^2 - 5x + 5$
		$\mathbf{A} f(x) = \begin{cases} 0 \text{ for } 0 < x < 3\\ 2 \text{ for } 3 < x < 6\\ 4 \text{ for } 6 < x < 9 \end{cases}$	
		$\mathbf{B} f(x) = \begin{cases} 0 \text{ for } 0 \le x < 3 \\ 2 \text{ for } 3 \le x < 6 \\ 4 \text{ for } 6 \le x < 9 \end{cases}$	
		C $f(x) = \begin{cases} 0 \text{ for } 0 < x \le 3 \\ 2 \text{ for } 3 < x \le 6 \\ 4 \text{ for } 6 < x \le 9 \end{cases}$	
		$\mathbf{D} f(x) = \begin{cases} 0 \text{ for } 0 \le x \le 3\\ 2 \text{ for } 3 \le x \le 6\\ 4 \text{ for } 6 \le x \le 9 \end{cases}$	

Instruction: Provide students an opportunity to analyze a step function and select its correct algebraic representation; and to analyze a table of values and determine the rule of the function.





A. Standard of Learning: A.II.9 The student will find the domain, range, zeros and inverse of a function, the value of a function for a given element in its domain, and the composition of multiple functions. Functions will include those that have domains and ranges that are limited and/or discontinuous. The graphing calculator will be used as a tool to assist in investigation of functions, including exponential and logarithmic.

Builds On: Students begin to work with the terms domain and range in grade 7 SOL and progress to finding the zeros of a function in the Algebra I SOL.

A	13	If $f(n) = 2^n - n$, then $f(3) =$	15	Which is a zero of the function $f(x) = x^2 + 6x + 8$?
		A 3		A ⁻ 8
		B 5		B -4
		C 9		с 2
		D 11		D 4
				D 4
	14	If the domain of $y + 2 = x^2$ is		
		$\{-2, -1, 1, 3\}$, what is the range?		
		F {-1, 2, 7}		
		G {-6, -3, 3, 11}		
		H $\{-7, -2, -1, 1\}$		
		b (11 , b , b , b)		

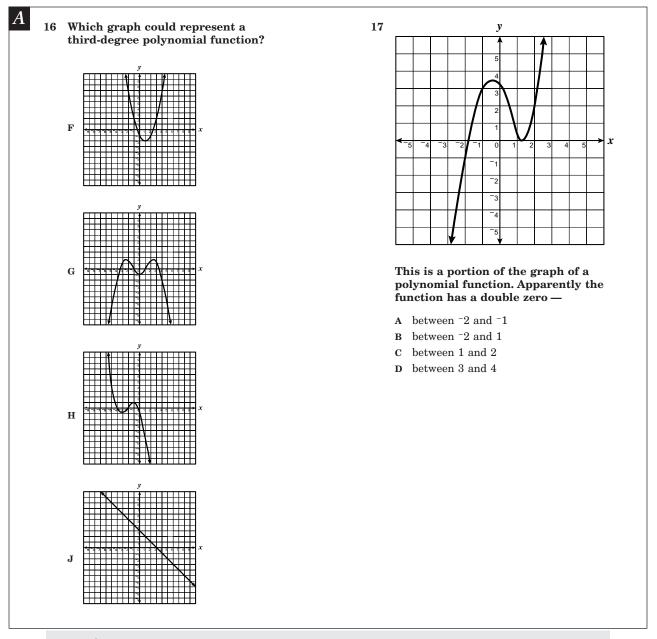
Instruction: Provide students an opportunity to find the zero of a linear function; to determine the range of a function when given the domain; and to find a composition of two functions.





A. Standard of Learning: A.II.15 The student will recognize the general shape of polynomial functions, locate the zeros, sketch the graphs, and verify graphical solutions algebraically. The graphing calculator will be used as a tool to investigate the shape and behavior of polynomial functions.

Builds On: Students begin working with polynomial functions in the Algebra I SOL.



Instruction: Provide students an opportunity to recognize the graph of a polynomial function, and find a zero of a function on a graph.



A



A. Standard of Learning: A.II.16 The student will investigate and apply the properties of arithmetic and geometric sequences and series to solve problems, including writing the first n terms, finding the nth term, and evaluating summation formulas. Notation will include Σ (Sigma) and a_n .

Builds On: Students begin analyzing numeric and geometric patterns in the grade 4 SOL and progress in complexity through the Algebra I SOL.

19

24 are –

A 8 and 12

B 8 and 16

C 9 and 16

D 10 and 17

Two arithmetic means between 3 and

18 Driving a piling into a harbor bottom, a pile driver sinks the piling 24 inches on the first stroke, 18 inches on the second stroke, and $13\frac{1}{2}$ inches on the third stroke. If the sequence is continued, how far will the piling be driven down on the 5th stroke?

F
$$1\frac{1}{2}$$
 in.
G $4\frac{1}{2}$ in.
H 6 in.

J
$$7\frac{19}{32}$$
 in

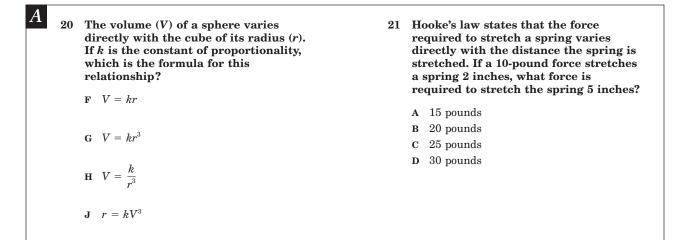
Instruction: Provide students an opportunity to find arithmetic means between two numbers in a sequence and the fifth term in a geometric sequence.





A. Standard of Learning: A.II.20 The student will identify, create, and solve practical problems involving a combination of direct and inverse variations.

Builds On: Students begin working with direct and inverse variations in the Algebra I SOL.



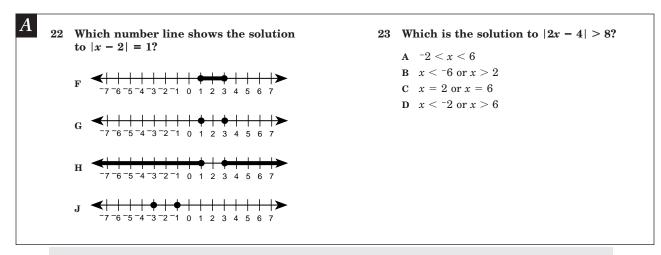
Instruction: Provide students an opportunity to solve problems involving direct variation.





A. Standard of Learning: A.II.4 The student will solve absolute value equations and inequalities graphically and algebraically. Graphing calculators will be used both as a primary method of solution and to verify algebraic solutions.

Builds On: Students begin solving equations in the grade 6 SOL and solving inequalities in the grade 7 SOL and progress through the Algebra I SOL.



Instruction: Provide students an opportunity to solve absolute value equations, and determine an absolute value inequality from a line graph.





A. Standard of Learning: A.II.6 The student will select, justify, and apply a technique to solve a quadratic equation over the set of complex numbers. Graphing calculators will be used for solving and confirming algebraic solutions.

Builds On: Students begin solving quadratic equations in the Algebra I SOL.

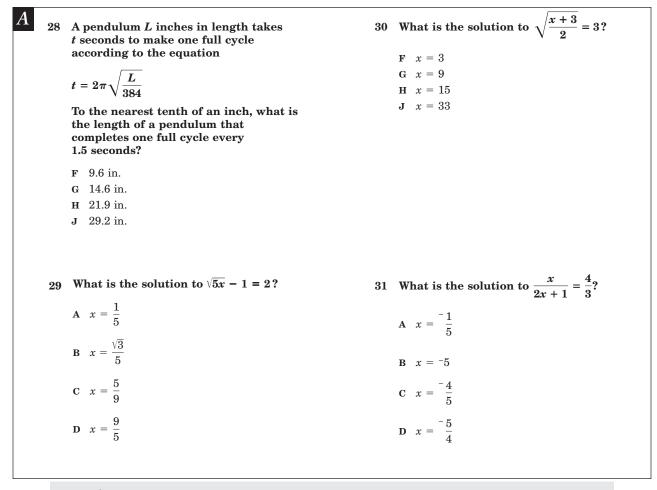
A 24 What are the solutions to 26 What are the solutions to $4x - 16 = -2x^2$? $(y + 3)^2 - 81 = 0?$ **F** x = 4i or x = -2**F** y = -12 or y = -6**G** x = -4 or x = 2**G** y = -12 or y = 6**H** x = 4 or x = 2i**H** y = 12 or y = -6**J** x = 4 or x = 2**J** y = 12 or y = 625 What are the solutions to 27 The height of a right triangle is 5 units $x^2 - 3x - 4 = 0?$ more than twice its base. If the area of the triangle is 21 square units, what is its height? **A** x = 1 or x = -4A $\frac{7}{2}$ units **B** x = -1 or x = 4B $\frac{-5 + \sqrt{193}}{4}$ units $\mathbf{C} \quad x = \frac{3 \pm i\sqrt{7}}{2}$ $c \quad \frac{5 + \sqrt{193}}{2}$ units $\mathbf{D} \quad x = \frac{3 \pm \sqrt{7}}{2}$ D 12 units

Instruction: Provide students an opportunity to find the solution set for a quadratic equation, and the complex number solution set for quadratic equations.



A. Standard of Learning: A.II.7 The student will solve equations containing rational expressions and equations containing radical expressions algebraically and graphically. Graphing calculators will be used for solving and confirming algebraic solutions.

Builds On: Students begin solving equations in the grade 6 SOL and progress through the Algebra I SOL.



Instruction: Provide students an opportunity to solve a problem with a formula containing a radical; to solve a rational equation; and to solve a radical equation.

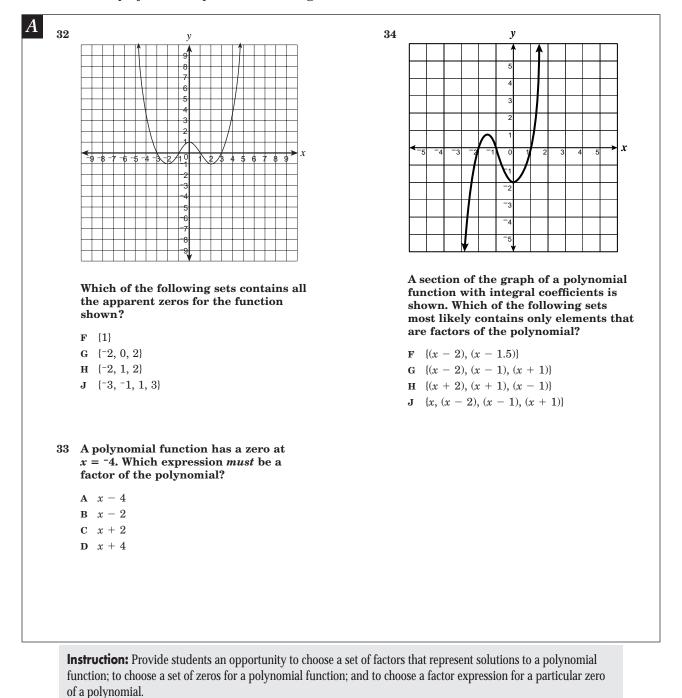




Reporting Category: Analytic Geometry

A. Standard of Learning: A.II.10 The student will investigate and describe the relationships between the solution of an equation, zero of a function, x-intercept of a graph, and factors of a polynomial expression through the use of graphs.

Builds On: Students begin to study the solutions of an equation, zero of a function, x-intercept of a graph, and factors of a polynomial expression in the Algebra I SOL.



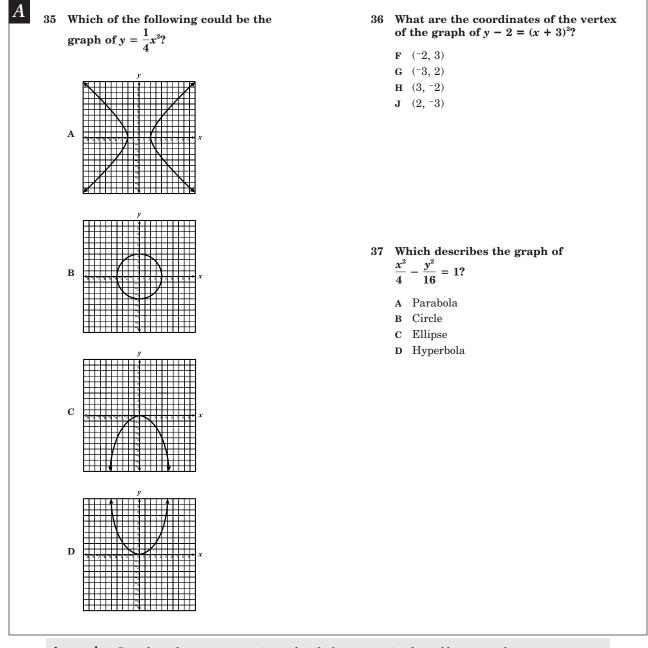
Algebra II



Reporting Category: Systems of Equations/Inequalities

A. Standard of Learning: A.II.18 The student will identify conic sections (circle, ellipse, parabola, and hyperbola) from his/her equations. Given the equations in (h, k) form, students will sketch graphs of conic sections, using transformations.

Builds On: Students begin to relate to equations and graphs in the grade 8 SOL and continue through the Algebra I SOL.



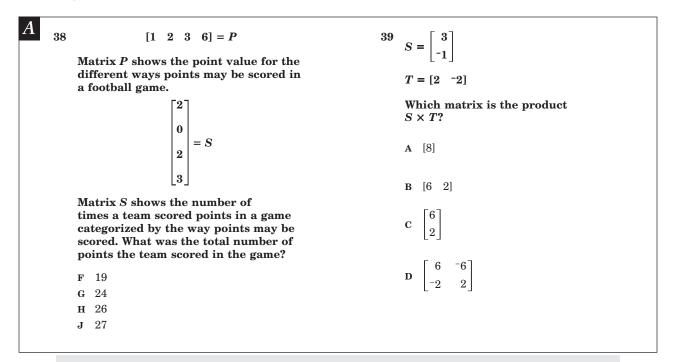
Instruction: Provide students an opportunity to identify the conic section formed by a particular equation; to choose the coordinates of the vertex of a particular equation; and to identify the conic section for a particular equation.





A. Standard of Learning: A.II.11 The student will use matrix multiplication to solve practical problems. Graphing calculators or computer programs with matrix capabilities will be used to find the product.

Builds On: Students begin to work with matrices in the grade 8 SOL and perform operations with matrices in the Algebra I SOL.



Instruction: Provide students an opportunity to find the product matrix when given two matrices.





A. Standard of Learning: A.II.12 The student will represent problem situations with a system of linear equations and solve the system using the inverse matrix method. Graphing calculators or computer programs with matrix capability will be used to perform computations.

Builds On: Students begin to work with matrices in the grade 8 SOL and perform operations with matrices in the Algebra I SOL.

A 40 If $A = \begin{bmatrix} 3 & 2 \\ 5 & 3 \end{bmatrix}$ and the product $A \cdot B = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$, then $B =$	 41 A small plant manufactures toy cars and trucks on two production lines. Matrix A is the input-output matrix of each item on each line per hour. Matrix B gives the number of hours each line operates in a day.
$\mathbf{F} \begin{bmatrix} \frac{1}{3} & 0\\ 0 & \frac{1}{3} \end{bmatrix}$	Line 1 Line 2 $A = \begin{bmatrix} 1 & 3 \\ 2 & 4 \end{bmatrix} Trucks$ Cars and Number of Hours $B = \begin{bmatrix} 8 \\ 12 \end{bmatrix}$
$\mathbf{G} \begin{bmatrix} -3 & 2\\ 5 & -3 \end{bmatrix}$ $\mathbf{H} \begin{bmatrix} \frac{1}{3} & \frac{1}{2}\\ \frac{1}{5} & \frac{1}{3} \end{bmatrix}$	Which product represents the matrix of the number of toy cars and trucks produced in a day on both production lines? A $\frac{Trucks}{Cars} \begin{bmatrix} 64\\ 44 \end{bmatrix}$
$\mathbf{J} \begin{bmatrix} 3 & -4 \\ 5 & -8 \end{bmatrix}$	$\begin{array}{c} Trucks \begin{bmatrix} 24\\ 72 \end{bmatrix} \\ Trucks \begin{bmatrix} 44 \end{bmatrix} \end{array}$
	$ \begin{array}{c} \mathbf{C} & Trucks \begin{bmatrix} 44\\ 64 \end{bmatrix} \\ \mathbf{D} & Trucks \begin{bmatrix} 16\\ Cars \end{bmatrix} \\ \end{array} $

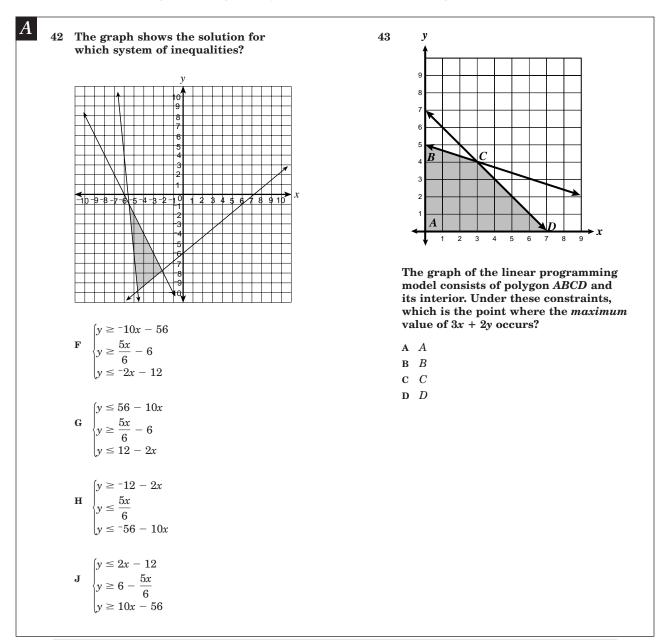
Instruction: Provide students an opportunity to find the inverse of a matrix and the solution matrix for a system of three linear equations.





A. Standard of Learning: A.II.13 The student will solve systems of linear inequalities and linear programming problems and describe the results both orally and in writing. A graphic calculator will be used to facilitate solutions to linear programming problems.

Builds On: Students begin working with systems of equations in the Algebra I SOL.



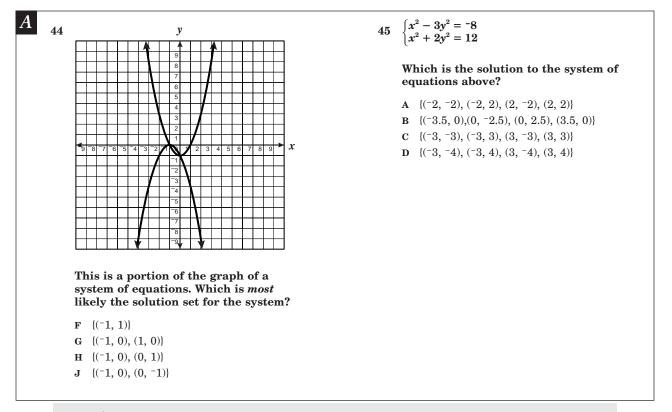
Instruction: Provide students an opportunity to determine the maximum value of a linear programming model's graph and select the system of inequalities that represents a given graph.





A. Standard of Learning: A.II.14 The student will solve nonlinear systems of equations, including linearquadratic and quadratic-quadratic, algebraically and graphically. The graphing calculator will be used as a tool to visualize graphs and predict the number of solutions.

Builds On: Students begin working with graphs of liens in the grade 8 SOL and with graphs of quadratics in the Algebra I SOL.



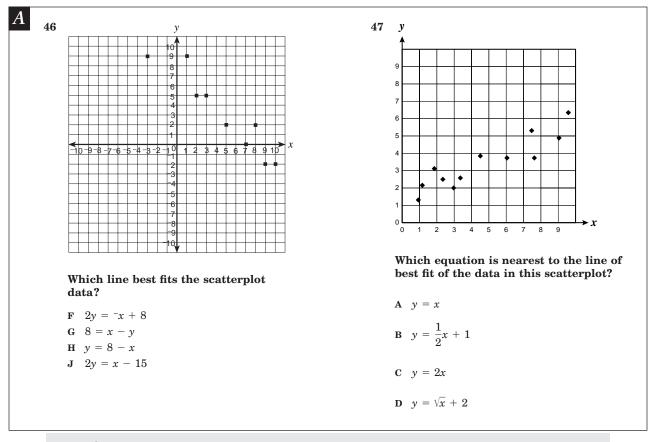
Instruction: Provide students an opportunity to identify the solution set for a system of quadratic equations from a graph and solve a system of linear-quadratic equations.





A. Standard of Learning: A.II.19 The student will collect and analyze data to make predictions, write equations, and solve practical problems. Graphing calculators will be used to investigate scatterplots to determine the equation for a curve of best fit.

Builds On: Students begin to collect, analyze data, and make predictions based on the data in the grade 2 SOL and progress to an investigation of scatterplots in the Algebra I SOL.



Instruction: Provide students an opportunity to identify an equation for a scatterplot graph.





A. Standard of Learning: A.II.19 The student will collect and analyze data to make predictions, write equations, and solve practical problems. Graphing calculators will be used to investigate scatterplots to determine the equation for a curve of best fit.

Builds On: Students begin to collect, analyze data, and make predictions based on the data in the grade 2 SOL and progress to an investigation of scatterplots in the Algebra I SOL.

- A 48 George was comparing the heights of 49 11 of his classmates with their algebra scores. Which of the following scatterplots is most likely a representation of that relationship? Score F • 0 Height Score • G • Height Score н Height Score J Height
 - 49 The table shows the number of students enrolled in the advanced algebra program at Fairoaks High School during the 6 years since its initiation.

Year (x)	Number of Students (n)			
1	66			
2	72			
3	82			
4	90			
5	100			
6	106			

Which of the following equations most closely describes the relationship between n, the number of students enrolled, and x, the number of years the class has been in existence?

A	n = x + 65
B	n=6x+60
С	n = 8x + 58
D	n = 10x + 46

- 50 In 1990, sales at ABC Electronics totaled 4.9 million dollars. During 1996, total sales amounted to 12.1 million. Assuming the growth in sales is a linear relation, what total sales can the company expect in 2001?
 - F 16.9 million
 - G 18.1 million
 - H 24.2 million
 - J 25.3 million

Instruction: Provide students an opportunity to predict a value from the graph of a scatterplot based on a line of best fit; to solve a practical problem using the line of best fit; to use a table of values to predict an amount; and to identify an equation for a scatterplot graph.

Correct Answers

Algebra II Test

1. C	2. J 3.	A 4.	H 5. 1	6. G	7. D	8. H	9. D	10. G
11. B	12. H	13. B	14. F	15. B	16. H	17. C	18. J	19. D
20. G	21. C	22. G	23. D	24. G	25. B	26. G	27. D	28. H
29. D	30. H	31. C	32. J	33. D	34. H	35. D	36. G	37. D
38. H	39. D	40. G	41. C	42. F	43. D	44. J	45. A	46. H
47. B	48. G	49. C	50. G					

