

Sudoku Puzzle with Derivatives  
(Basic derivative formulas, Chain Rule, Implicit differentiation)  
A Puzzle by David Pleacher

Solve the 26 derivative problems below and place the answer in the corresponding cell (labeled A, B, C, ... Y, Z). Your answers should be integers from 1 to 9 inclusive. Then solve the resulting SUDOKU puzzle.

The rules of Sudoku are simple.

Enter digits from 1 to 9 into the blank spaces.

Every row must contain one of each digit.

So must every column, and so must every 3x3 square.

Each Sudoku has a unique solution that can be reached logically without guessing.

Thanks to Angelica Vialpando and her students for finding the error in Clue #X.

---

A. Determine  $\frac{d}{dx}(8x) =$

B. Given  $y = x^3 - x^2 + x - 4$ , determine the value of  $\frac{dy}{dx}$  when  $x = -1$ .

C. Determine the value of  $\left. \frac{dy}{dx} \right|_{x=4}$  if  $y = 21\sqrt{2x+1}$

D. Determine the value of  $f'(1)$  if  $f(x) = \frac{-9}{x-2}$

E. Determine the value of  $\left. \frac{dy}{dx} \right|_{x=8}$  if  $y = 36x^{\frac{1}{3}}$

F. Given  $y = \frac{2x-3}{3x+4} - 10x$ , determine the value of  $\frac{dy}{dx}$  when  $x = -1$

G. Determine  $\frac{ds}{dt}$ , given that  $s = 6t - 3$

H. Determine  $h'(1.5)$  if  $h(x) = x^2 + 2x - 3$

I. Given  $s = \frac{1}{2t^2}$ , determine  $\frac{ds}{dt}$  when  $t = -\frac{1}{2}$

- J. Determine the value of the derivative  $\frac{dy}{dx}$  at  $x = -2$ , given that  $y = \frac{-6}{x+1}$
- K. If  $y = 36\sqrt{x}$ , determine the value of  $\frac{dy}{dx}\Big|_{x=4}$
- L. Determine the derivative of  $y = |x|$  at  $x = 13$ .
- M. If  $s$  is measured in feet and  $t$  in seconds, determine the velocity at time  $t = 2$  of the motion  $s = t^2 + 3t$ .
- N. If  $y = 3\sqrt{1+2x}$ , Determine the value of  $\frac{dy}{dx}\Big|_{x=0}$
- O. If  $f(x) = \frac{-8}{\sqrt{2+x}}$ , determine the value of  $f'(-1)$ .
- P. Evaluate  $f'(0)$  if  $f(x) = e^{4x}$ .
- Q. Determine the x-coordinate of the vertex of the parabola  $y = x^2 - 4x + 1$  by making use of the fact that at the vertex the slope of the tangent is zero.
- R. Given  $y = \frac{-(1-5x)^6}{6}$ , determine the value of  $\frac{dy}{dx}$  when  $x = 0$ .
- S. Determine the slope of the tangents to the parabola  $y = -x^2 + 5x - 6$  at its points of intersection with the x-axis. Use only the positive slope in the SUDOKU.
- T. Determine the value of  $\frac{d^3y}{dx^3}\Big|_{x=0}$  if  $y = \frac{1}{5}x^5 + \frac{1}{6}x^3 - 2x^2 + 17x - 9$
- U. A point moves in the plane according to the law  $x = t^2 + 2t$  and  $y = \frac{8}{3}t^3 - 8t$ .  
Determine  $\frac{dy}{dx}$  when  $t = 3$ .
- V. If  $y = \ln(x+3)^2$ , determine the value of  $\frac{dy}{dx}$  when  $x = -2$ .

W. Given  $f(x) = \frac{1}{18}(2x-1)^3(3x+4)^2$ , determine  $f'(0)$ .

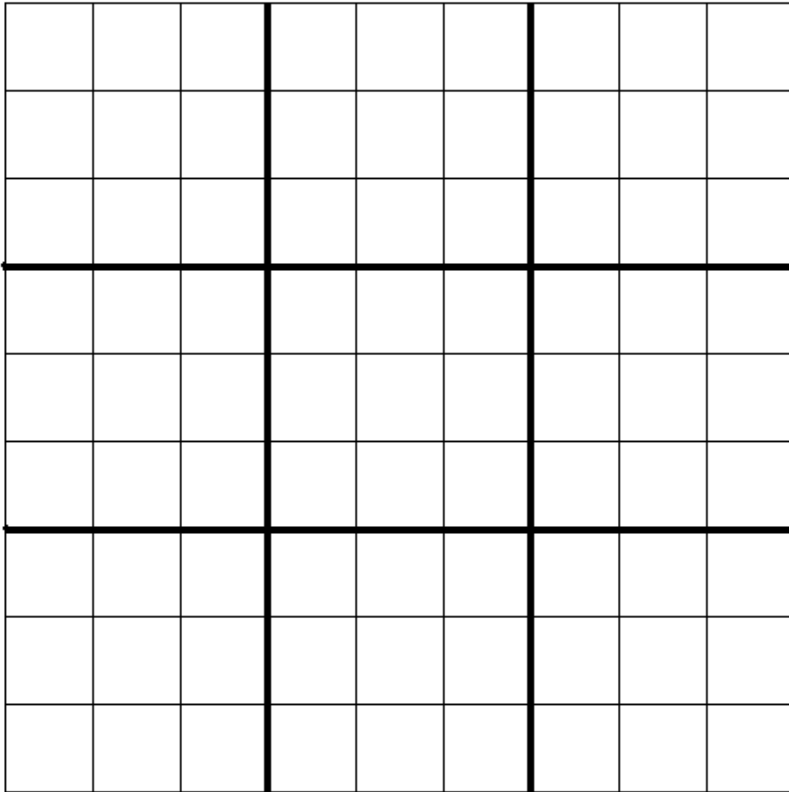
X. If  $xy = -4$ , determine the value of  $\frac{dy}{dx}$  at the point  $(-\sqrt{2}, 2\sqrt{2})$ .

Y. Evaluate  $\left. \frac{dy}{dx} \right|_{x=1}$  if  $y = \frac{448}{5} \left( \frac{x}{1+x} \right)^5$ .

Z. Determine the value of  $g'(0)$  if  $g(x) = \frac{3x-1}{3x+1}$

	<b>A</b>	<b>B</b>					<b>C</b>	<b>D</b>
		<b>E</b>		<b>F</b>				<b>G</b>
			<b>H</b>			<b>I</b>		
			<b>J</b>			<b>K</b>		
	<b>L</b>		<b>M</b>		<b>N</b>		<b>O</b>	
		<b>P</b>			<b>Q</b>			
		<b>R</b>			<b>S</b>			
<b>T</b>				<b>U</b>		<b>V</b>		
<b>W</b>	<b>X</b>					<b>Y</b>	<b>Z</b>	

Here is a blank SUDOKU board for you to use:



## Solution to the Sudoku With Derivatives Puzzle

$$A = 8$$

$$B = 6$$

$$C = 7$$

$$D = 9$$

$$E = 3$$

$$F = 7$$

$$G = 6$$

$$H = 5$$

$$I = 8$$

$$J = 6$$

$$K = 9$$

$$L = 1$$

$$M = 7$$

$$N = 3$$

$$O = 4$$

$$P = 4$$

$$Q = 2$$

$$R = 5$$

$$S = 1$$

$$T = 1$$

$$U = 8$$

$$V = 2$$

$$W = 4$$

$$X = 2$$

$$Y = 7$$

$$Z = 6$$

<b>2</b>	<b>8</b>	<b>6</b>	<b>3</b>	<b>1</b>	<b>4</b>	<b>5</b>	<b>7</b>	<b>9</b>
<b>5</b>	<b>4</b>	<b>3</b>	<b>8</b>	<b>7</b>	<b>9</b>	<b>1</b>	<b>2</b>	<b>6</b>
<b>9</b>	<b>7</b>	<b>1</b>	<b>5</b>	<b>2</b>	<b>6</b>	<b>8</b>	<b>3</b>	<b>4</b>
<b>3</b>	<b>5</b>	<b>7</b>	<b>6</b>	<b>4</b>	<b>8</b>	<b>9</b>	<b>1</b>	<b>2</b>
<b>8</b>	<b>1</b>	<b>2</b>	<b>7</b>	<b>9</b>	<b>3</b>	<b>6</b>	<b>4</b>	<b>5</b>
<b>6</b>	<b>9</b>	<b>4</b>	<b>1</b>	<b>5</b>	<b>2</b>	<b>3</b>	<b>8</b>	<b>7</b>
<b>7</b>	<b>3</b>	<b>5</b>	<b>2</b>	<b>6</b>	<b>1</b>	<b>4</b>	<b>9</b>	<b>8</b>
<b>1</b>	<b>6</b>	<b>9</b>	<b>4</b>	<b>8</b>	<b>7</b>	<b>2</b>	<b>5</b>	<b>3</b>
<b>4</b>	<b>2</b>	<b>8</b>	<b>9</b>	<b>3</b>	<b>5</b>	<b>7</b>	<b>6</b>	<b>1</b>